# Absolute Momentum: a Simple Rule-Based Strategy and Universal Trend-Following Overlay

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## **Abstract**

There is a considerable body of research on relative strength price momentum but relatively little on absolute, time series momentum. In this paper, we explore the practical side of absolute momentum. We first explore its sole parameter - the formation, or look back, period. We then examine the reward, risk, and correlation characteristics of absolute momentum applied to stocks, bonds, and real assets. We finally apply absolute momentum to a 60-40 stock/bond portfolio and a simple risk parity portfolio. We show that absolute momentum can effectively identify regime change and add significant value as an easy to implement, rule-based approach with many potential uses as both a stand- alone program and trend following overlay.

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### 1. Introduction

The cross-sectional momentum effect is one of the strongest and most pervasive financial phenomena (Jegadeesh and Titman (1993), (2001)). Researchers have verified its value with many different asset classes, as well as across groups of assets (Blitz and Van Vliet (2008), Asness, Moskowitz and Pedersen (2012)). Since its publication, momentum has held up out-of-sample going forward in time (Grundy and Martin (2001), Asness, Moskowitz and Pedersen (2012)) and back to the Victorian Age (Chabot, Ghysels, and Jagannathan (2009)).

In addition to cross-sectional momentum, in which an asset's performance relative to other assets predicts its future relative performance, momentum also works well on an absolute, or time series basis, in which an asset's own past return predicts its future performance. In absolute momentum there is significant positive auto-covariance between an asset's excess return next month and its lagged one-year return (Moskowitz, Ooi and Pedersen (2012)).

Absolute momentum is therefore trend following by nature. Trend following methods, in general, have slowly achieved recognition and acceptance in the academic community (Brock, Lakonishok and LeBaron (1992), Lo, Mamaysky, and Wang (2000), Zhu and Zhou (2009), Han, Yang, and Zhou (2011)).

Absolute momentum appears to be just as robust and universally applicable as cross-sectional momentum. It performs well in extreme market environments, across

multiple asset classes (commodities, equity indices, bond markets, currency pairs), and back in time to the turn of the century (Hurst, Ooi, and Pedersen (2012)).

Despite an abundance of momentum research over the past twenty years, no one is sure why it works so well. The most common explanations for both momentum and trend following profits have to do with behavioral factors, such as anchoring, herding, and the disposition effect (Tversky and Kahneman (1974), Barberis, Shleifer, and Vishny (1998), Daniel, Hirshleifer, and Subrahmanyam (1998), Hong and Stein (1999), Frazzini (2006)).

In anchoring, investors are slow to react to new information, which leads initially to under reaction. In herding, buying begets more buying and causes prices to over react and move beyond fundamental value after the initial under reaction. Through the disposition effect, investors sell winners too soon and hold losers too long. This creates a headwind making trends continue longer before reaching true value.

Risk management schemes that sell in down markets and buy in up markets can also cause trends to persist (Garleanu and Pedersen (2007)), as can confirmation bias, which causes investors to look at recent price moves as representative of the future. This then leads them to move money into investments that have recently appreciated, thus causing trends to continue further (Tversky and Kahneman (1974)). Behavioral biases are deeply rooted, which may explain why momentum profits have persisted and are likely to continue to persist.

In this paper, we focus on absolute momentum because of its simplicity and the advantages it holds for long-only investing. We can apply absolute momentum to any asset or portfolio of assets without losing any of the contributory value of other assets. With relative strength momentum, on the other hand, we have to exclude weaker assets from the active portfolio. This can reduce the benefits that come from multi-asset diversification and create opportunity loss by excluding assets that may suddenly start outperforming.

The second advantage of absolute momentum is its superior ability to reduce downside volatility and drawdown by identifying regime change. Both relative and absolute momentum can enhance return, but absolute momentum, by its trend-following nature, is much more effective in reducing the downside exposure associated with long-only investing (Antonacci (2013)).

The next section of this paper describes our data and the methodology we use to work with absolute momentum. The following section explores the formation period used for determining absolute momentum. After that, we show what effect absolute momentum has on the reward, risk, and correlation characteristics of a number of diverse markets, compared to a buy and hold approach. Finally, we apply absolute momentum to two representative multi-asset portfolios - a 60-40 balanced stock/bond portfolio and a simple, diversified risk parity portfolio.

# 2. Data and Methodology

All monthly data begins in January 1973, unless otherwise noted, and includes interest and dividends. For equities, we use the MSCI US and MSCI EAFE (Europe, Australia, and Far East) indices. These are free float adjusted market capitalization weightings of large and midcap stocks. The MSCI EAFE index includes twenty-two major developed market countries, excluding the U.S. and Canada. For fixed income, we use the Barclays Capital Long U.S. Treasury, Intermediate U.S. Treasury, U.S. Credit, U.S. High Yield Corporate, U.S. Government & Credit, and U.S. Aggregate Bond indices. The beginning date of the high yield index is July 1, 1983, and the start date of the aggregate bond index is January 1, 1976. For dates prior to January 1976, we substitute the Government & Credit index for the Aggregate Bond index, since they track one another very closely. For Treasury bills, we use the monthly returns on 90-day U.S. Treasury bill holdings. For real assets, we use the FTSE NAREIT U.S. Real Estate index, the Standard & Poor's GSCI (formally Goldman Sachs Commodities Index), and monthly gold returns based on the month-end closing London PM gold fix.

Although there are more complicated methods for determining absolute momentum (Baltas and Kosowski (2012)), our strategy simply defines absolute momentum as being positive when the excess return (asset return less the Treasury bill return) over the formation, or look back, period is positive. We hold a long position in our selected assets during these times. When absolute momentum turns negative (i.e., an asset's

excess return turns negative), our baseline strategy is to exit the asset and switch into 90-day U.S. Treasury bills until absolute momentum again becomes positive. Treasury bills are a safe harbor for us during times of market stress.

We reevaluate and adjust positions on a monthly basis. The number of transactions per year into or out of Treasury bills ranges from a low of 0.33 for REITs to a high of 1.08 for high yield bonds. We deduct 20 basis points per trade for transaction costs.

Maximum drawdown is the greatest peak-to-valley equity erosion on a month-end basis.

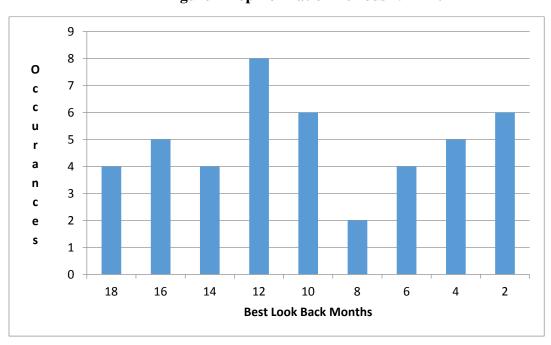
### 3. Formation Period

Table 1 shows the Sharpe ratios for a range of formation periods ranging from 2 to 18 months. Since our data begins in January 1973 (except for high yield bonds, which begin in July 1983) and 18 months is the maximum formation period that we consider, results extend from July 1974 through December 2012. We have highlighted the highest Sharpe ratios for each asset.

**Table 1 Formation Period Sharpe Ratios** 

|         | 18  | 16  | 14  | 12  | 10  | 8   | 6   | 4   | 2   |
|---------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
|         |     |     |     |     |     |     |     |     |     |
| MSCI US | .41 | .43 | .45 | .56 | .46 | .44 | .41 | .38 | .23 |
| EAFE    | .33 | .32 | .35 | .41 | .45 | .32 | .38 | .36 | .46 |
| TBOND   | .40 | .42 | .45 | .54 | .38 | .36 | .33 | .42 | .40 |
| CREDIT  | .75 | .80 | .70 | .74 | .80 | .81 | .69 | .71 | .66 |
| HI YLD  | .70 | .87 | .82 | .92 | .66 | .69 | .82 | .77 | .77 |
| REIT    | .65 | .71 | .72 | .69 | .63 | .63 | .87 | .68 | .63 |
| GSCI    | .04 | .04 | .09 | .20 | .09 | 08  | 11  | .13 | .06 |
| GOLD    | .39 | .35 | .35 | .42 | .39 | .37 | .32 | .30 | .21 |

Best results cluster at 12 months.<sup>2</sup> As a check on this, we segment our data into subsamples and find the highest Sharpe ratios for each asset in every decade from 1974 through 2012. Figure 1 shows the number of times the Sharpe ratio is highest (or within two percentage points of being the highest) for each look back period across all the decades.



**Figure 1 Top Formation Periods 1974-2012** 

Our results coincide with the best formation periods of cross-sectional momentum, which extend from 3 to 12 months and also cluster at 12 months<sup>3</sup> (Jegadeesh and Titman (1993)). Many momentum papers use a 12-month formation period with a 1-

<sup>&</sup>lt;sup>2</sup> We looked at monthly moving average penetrations as an alternative trend following filter and found no discernible pattern of optimal values.

pattern of optimal values. <sup>3</sup> Cowles and Jones (1937) were the first to point out the profitable look back period of 12 months using U.S. stock market data from 1920 through 1935.

month holding period as a benchmark strategy for research purposes. Given its dominance here and throughout the literature, we will also use a 12-month formation period as our benchmark strategy. This should minimize the risk of data snooping.

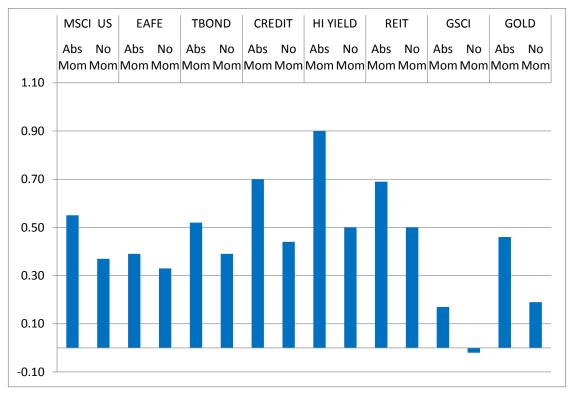
## 4. Absolute Momentum Characteristics

Table 2 is a performance summary of each asset and the median of all the assets, with and without 12-month absolute momentum.

**Table 2 Absolute Momentum Results 1974-2012** 

|                 | Annual | Annual  | Annual | Maximum  | % Profit |
|-----------------|--------|---------|--------|----------|----------|
|                 | Return | Std Dev | Sharpe | Drawdown | Months   |
| MSCI US Abs Mom | 12.26  | 11.57   | .55    | -22.90   | 75       |
| MSCI US No Mom  | 11.62  | 15.74   | .37    | -50.65   | 61       |
| EAFE Abs Mom    | 10.39  | 11.82   | .39    | -25.14   | 78       |
| EAFE No Mom     | 11.56  | 17.53   | .33    | -56.40   | 60       |
| TBOND Abs Mom   | 10.08  | 8.43    | .52    | -12.92   | 77       |
| TBOND No Mom    | 9.74   | 10.54   | .39    | -20.08   | 61       |
| CREDIT Abs Mom  | 8.91   | 4.72    | .70    | -8.70    | 82       |
| CREDIT No Mom   | 8.77   | 7.18    | .44    | -19.26   | 67       |
| HI YLD Abs Mom  | 9.97   | 4.76    | .90    | -7.14    | 88       |
| HI YLD No Mom   | 10.05  | 8.70    | .50    | -33.31   | 75       |
| REIT Abs Mom    | 14.16  | 11.74   | .69    | -19.97   | 75       |
| REIT No Mom     | 14.74  | 17.25   | .50    | -68.30   | 62       |
| GSCI Abs Mom    | 8.24   | 15.46   | .17    | -48.93   | 81       |
| GSCI No Mom     | 4.93   | 19.96   | 02     | -61.03   | 54       |
| GOLD Abs Mom    | 13.68  | 16.62   | .46    | -24.78   | 81       |
| GOLD No Mom     | 9.44   | 19.97   | .19    | -61.78   | 53       |
| MEDIAN Abs Mom  | 10.25  | 11.66   | .53    | -21.43   | 79       |
| MEDIAN No Mom   | 9.90   | 16.48   | .38    | -53.53   | 61       |

Figure 2 shows the Sharpe ratios and percentage of profitable months for these assets, with and without 12-month absolute momentum. Figure 3 presents the percentage of profitable months, and Figure 4 shows maximum monthly drawdown. Every asset has a higher Sharpe ratio, lower maximum drawdown, and higher



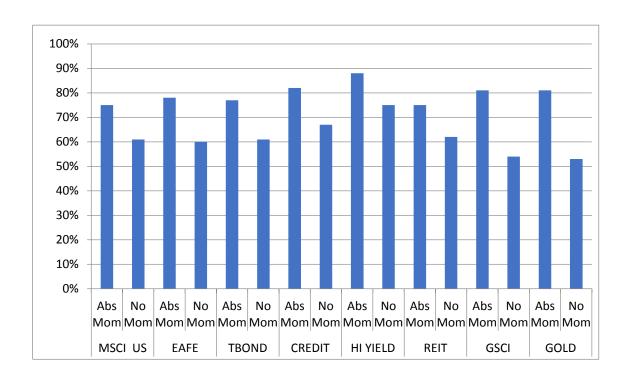
percentage of profitable months with 12-absolute momentum over this 38-year period.

Figure 2 Sharpe Ratios 1974-2012<sup>4</sup>

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<sup>&</sup>lt;sup>4</sup> The percentage of months each asset has positive absolute momentum: MSCI US 72%, MSCI EAFE 65%, TBOND 66%, CREDIT 56%, HI YIELD 68%, REIT 78%, GSCI 50%, and GOLD 53%.



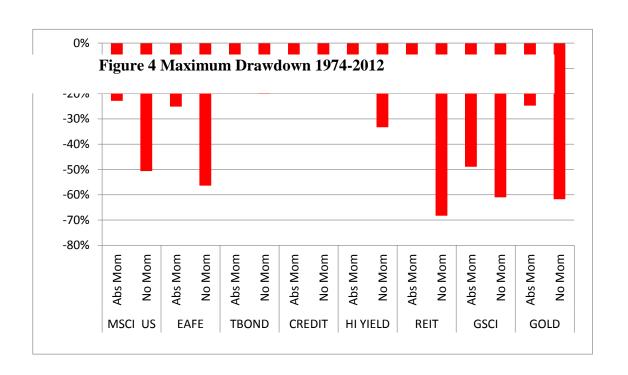


Table 3 shows the monthly correlations between our assets, with and without the application of absolute momentum. The average correlation of the eight assets without absolute momentum is .22, and with absolute momentum, it is .21. There is no indication from our data that absolute momentum, in general, increases correlation. This has positive implications for applying absolute momentum to multi-asset portfolios, which we pursue in the next section.

**Table 3 Monthly Correlation and Momentum 1974-2012** 

| No Momentum |      |         |            |           |      |      |      |  |
|-------------|------|---------|------------|-----------|------|------|------|--|
|             | EAFE | TBOND   | CREDIT     | HI YLD    | REIT | GSCI | GOLD |  |
| MSCI US     | .63  | .11     | .26        | .43       | .58  | .10  | .01  |  |
| EAFE        |      | .03     | .12        | .37       | .48  | .18  | .19  |  |
| TBOND       |      |         | .67        | .12       | .05  | 10   | .01  |  |
| CREDIT      |      |         |            | .40       | .15  | .04  | 02   |  |
| HI YLD      |      |         |            |           | .32  | .07  | 04   |  |
| REIT        |      |         |            |           |      | .11  | .07  |  |
| GSCI        |      |         |            |           |      |      | .27  |  |
|             |      | w/ 12-M | onth Absol | ute Momer | ntum |      |      |  |
|             | EAFE | TBOND   | CREDIT     | HI YLD    | REIT | GSCI | GOLD |  |
| MSCI US     | .49  | .05     | .35        | .45       | .45  | .14  | .04  |  |
| EAFE        |      | .03     | .26        | .31       | .29  | .13  | .11  |  |
| TBOND       |      |         | .81        | .04       | 03   | 04   | 02   |  |
| CREDIT      |      |         |            | .38       | .28  | 01   | .05  |  |
| HI YLD      |      |         |            |           | .41  | .09  | .02  |  |
| REIT        |      |         |            |           |      | .13  | .12  |  |
| GSCI        |      |         |            |           |      |      | .30  |  |

### 5. 60-40 Balanced Portfolio

Given the ability of 12-month absolute momentum to improve risk-adjusted performance over a broad range of individual assets, it is natural to wonder what effect absolute momentum might have on multi-asset portfolios. One of the earliest and simplest multi-asset portfolios is the 60% stocks and 40% bonds mix that institutional investors adopted in the mid-1960s, based on their observation of stock and bond returns from 1926 through 1965. Table 4 shows how a 60-40 portfolio of the US MSCI and Long US Treasury indices has performed since 1974, with and without the addition of 12-month absolute momentum.

Table 4 60-40 Portfolio Performance 1974-2012

|           | Annual | Annual  | Annual | Maximum  | % Profit | Correlation | Correlation to |
|-----------|--------|---------|--------|----------|----------|-------------|----------------|
|           | Return | Std Dev | Sharpe | Drawdown | Months   | to S&P500   | 10 Yr Bond     |
| 60-40     | 11.52  | 7.88    | .72    | -13.45   | 74       | .67         | .37            |
| w/Abs Mom |        |         |        |          |          |             |                |
| 60-40     | 10.86  | 10.77   | .47    | -29.32   | 63       | .92         | .46            |
| No Mom    |        |         |        |          |          |             |                |
| MSCI US   | 12.26  | 11.57   | .55    | -22.90   | 75       | .74         | .13            |
| w/Abs Mom |        |         |        |          |          |             |                |
| MSCI US   | 11.62  | 15.74   | .37    | -50.65   | 61       | 1.00        | .10            |
| No Mom    |        |         |        |          |          |             |                |

The regular 60-40 portfolio without momentum shows some reduction in volatility and drawdown compared to an investment solely in US stocks. However, the strong .92 correlation of the regular momentum 60-40 portfolio with the S&P 500 shows that the 60-40 portfolio has retained most of the market risk of stocks. Because stocks are much more volatile than bonds, stock market movement dominates the risk in

a 60-40 portfolio. From a risk perspective, the regular 60/40 portfolio is, in fact, mainly an equity portfolio, since stock market variation explains nearly all the variation in performance of the regular 60-40 portfolio.

The MSCI US index with the addition of absolute momentum has a .74 correlation to the S&P 500 index, which is lower than the correlation of the regular 60-40 index. It does a better job than the 60-40 portfolio in reducing portfolio drawdown, while also providing higher returns. The correlation to the S&P 500 of the 60-40 portfolio using 12-month absolute momentum drops to .67, indicating more reduction in stock market exposure. The 60-40 portfolio with absolute momentum retains the same return as the normal MSCU US index, but with only half the volatility. The maximum drawdown drops by more than 70%.

Figure 5 shows the maximum 3, 6, and 12-month drawdowns of the MSCI US index and the 60-40 portfolios, with and without 12-month absolute momentum. Figure 6 is a rolling 5-year window of the maximum drawdown of the same portfolios.

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<sup>&</sup>lt;sup>5</sup> During the 10 years ending December 2012, the correlation of the absolute momentum 60-40 portfolio to the S&P 500 index was .53, compared to a correlation of .87 for the normal 60-40 portfolio to the S&P 500 index.

Figure 5 1 to 12 Month Maximum Drawdown 1974-2012

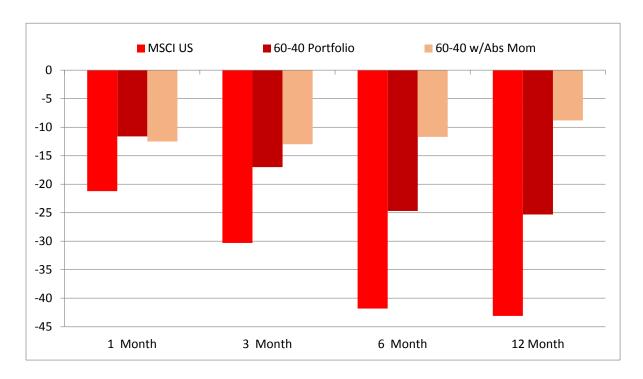
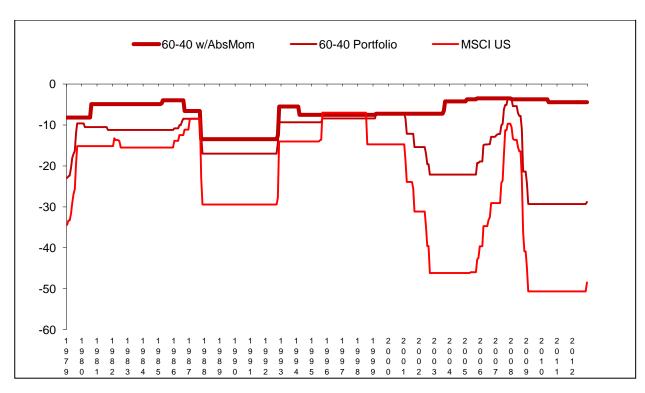


Figure 6 Rolling 5 Year Maximum Drawdown 1979-2012

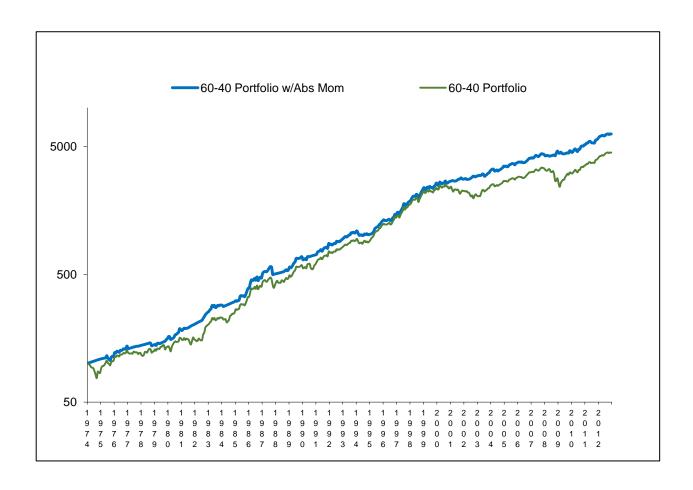


The traditional 60-40 portfolio offers little in the way of risk-reducing diversification, even though it looks balanced from the perspective of dollars invested in each asset class. From 1900 through 2012, the probability of the 60-40 portfolio having a negative real return has been 35% in any one year, 20% over any 5 years, and 10% over any 10 years<sup>6</sup>. Adding a simple 12-month absolute momentum overlay to the 60-40 portfolio may be all that is necessary to achieve market level returns with a more reasonable amount of downside risk. Figure 7 shows the consistency of the 12-month absolute momentum 60-40 portfolio compared to the traditional 60-40 portfolio. The chart also shows that the trend following, market-timing feature of absolute momentum may be more valuable now than in the past, when the world was less inter-connected, asset correlations were lower, and diversification alone was better able to reduce downside exposure.

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<sup>&</sup>lt;sup>6</sup> Data from the Robert Schiller website: http://www.econ.yale.edu/~shiller/data.htm

Figure 7 60-40 Portfolios 1974-2012



# **6. Parity Portfolios**

The usual way of dealing with the strong equities tilt and risk of the 60-40 portfolio is to diversify more broadly and/or to dedicate a larger allocation to fixed income investments. Endowment funds, for example, often diversify into a number of specialized areas, such as private equity, hedge funds, and other high risk alternative investments. Some risk parity programs also diversify broadly. In addition, risk parity portfolios attempt to equalize the risk across different asset classes by allocating more

to lower volatility assets. A stock-bond only portfolio, for example, would require at least a 70% allocation to bonds in order to have equal risk from bonds and equities.

We can construct a simple, monthly-rebalanced risk parity portfolio and apply 12-month absolute momentum to it. Starting with the same MSCI US and long Treasury bond indices used in our 60-40 portfolio, we add REITs, credit bonds, and gold, with an equal weighting given to all. We use credit bonds to increase the low-volatility, fixed income side of the portfolio. Credit bonds also diversify our fixed income allocation by providing credit risk premium and less duration risk than long Treasuries. REITs give exposure to real assets and equities. Gold has the highest volatility, and so represents only 20% of the portfolio, whereas equities and fixed income make up the majority of portfolio assets. Table 5 shows the correlations of the S&P 500, U.S.10 Year Treasury, and GSCI Commodity indices to the 60-40 and Parity Portfolios, both with and without 12-month absolute momentum.

**Table 5 Monthly Correlations 1974-2012** 

|              | 60-40<br>Portfolio | 60-40 w/Abs<br>Momentum | Parity<br>Portfolio | Parity w/Abs<br>Momentum |
|--------------|--------------------|-------------------------|---------------------|--------------------------|
| S&P 500      | .92                | .67                     | .67                 | .40                      |
| 10 Year Bond | .58                | .35                     | .37                 | .36                      |
| GSCI         | .05                | .06                     | .25                 | .19                      |

<sup>&</sup>lt;sup>7</sup> We use gold instead of commodities because of the possible lack of risk premia and the substantial front-running rollover costs associated with commodity index futures contracts (Daskalaki and Skiadopoulus (2011), Mou (2011)).

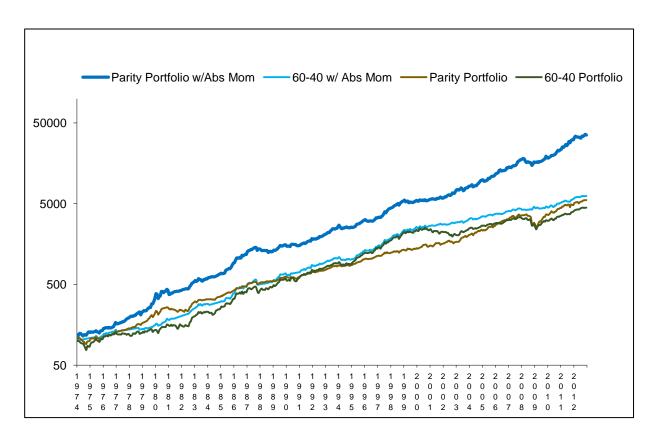
Our Parity Portfolio with 12-month absolute momentum shows a modest and nearly equal correlation to both stocks and bonds. Because of the downside risk attenuation through absolute momentum, we have achieved risk parity while limiting fixed income to only 40% of our assets. Having a well-balanced portfolio means that in low growth and low inflation environments, gold and bonds may outperform and sustain the portfolio, whereas equities and REITs may perform better under high inflation and high growth scenarios. Table 6 shows the comparative performance of the 60-40 and Parity Portfolios, with and without 12-month absolute momentum.

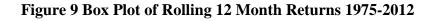
Table 6 Parity Portfolios versus 60-40 Portfolios 1974-2012

|                 | Parity w/Abs Mom | Parity Portfolio | 60-40 w/Abs Mom | 60-40 Portfolio |
|-----------------|------------------|------------------|-----------------|-----------------|
| All Data        |                  |                  |                 |                 |
| Annual Return   | 11.98            | 11.28            | 11.52           | 10.86           |
| Annual Std Dev  | 5.75             | 8.88             | 7.88            | 10.77           |
| Annual Sharpe   | 1.06             | 0.62             | 0.72            | 0.47            |
| Max Drawdown    | -9.60            | -30.40           | -13.45          | -29.32          |
| % Profit Months | 75               | 69               | 74              | 63              |
| 1974-83         |                  |                  |                 |                 |
| Annual Return   | 15.78            | 13.10            | 11.37           | 9.41            |
| Annual Std Dev  | 7.20             | 10.05            | 6.88            | 12.35           |
| Annual Sharpe   | 0.86             | 0.38             | 0.33            | 0.04            |
| Max Drawdown    | -6.31            | -16.89           | -8.19           | -22.95          |
| % Profit Months | 80               | 64               | 81              | 52              |
| 1984-93         |                  |                  |                 |                 |
| Annual Return   | 12.34            | 10.19            | 14.48           | 15.63           |
| Annual Std Dev  | 4.98             | 5.62             | 9.78            | 11.40           |
| Annual Sharpe   | 1.09             | 0.62             | 0.75            | 0.73            |
| Max Drawdown    | -4.28            | -6.53            | -13.45          | -16.99          |
| % Profit Months | 78               | 71               | 79              | 68              |

| 1994-03         |       |        |       |        |
|-----------------|-------|--------|-------|--------|
| Annual Return   | 9.06  | 9.45   | 12.10 | 10.86  |
| Annual Std Dev  | 4.65  | 6.66   | 8.23  | 10.05  |
| Annual Sharpe   | 0.99  | 0.74   | 0.90  | 0.62   |
| Max Drawdown    | -4.87 | -7.56  | -8.16 | -22.14 |
| % Profit Months | 72    | 73     | 69    | 64     |
| 2004-12         |       |        |       |        |
| Annual Return   | 10.69 | 12.55  | 7.84  | 7.34   |
| Annual Std Dev  | 5.78  | 12.12  | 5.92  | 8.80   |
| Annual Sharpe   | 1.47  | 0.84   | 0.99  | 0.61   |
| Max Drawdown    | -9.60 | -30.40 | -5.03 | -29.32 |

Figure 8 Parity and 60-40 Portfolios 1974-2012





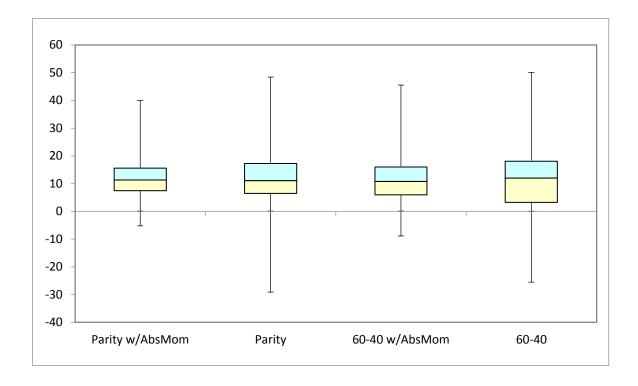
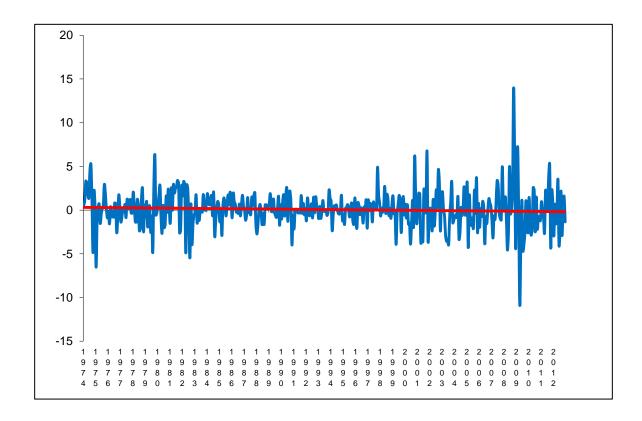


Figure 9 is a box plot showing quartile ranges of rolling 12-month portfolio returns. Figure 10 shows the difference in monthly returns between the Parity Portfolios with and without 12-month absolute momentum. There was some increased volatility in 2008-2009. However, the plotted trend line shows the return differences remained constant over time.

Figure 10 Monthly Differences in Parity Portfolio Performance 1974-2012



# 7. Parity Portfolio Drawdown

As was the case with individual assets and the 60-40 portfolio, 12-month absolute momentum excels in reducing the Parity Portfolio drawdown, as per Figures 11-12

Figure 11 1 to 12 Month Maximum Drawdown 1974-2012

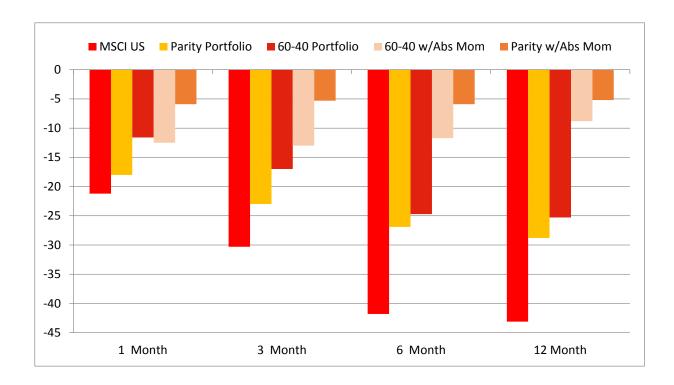


Figure 12 Rolling 5 Year Maximum Drawdown 1979-2012

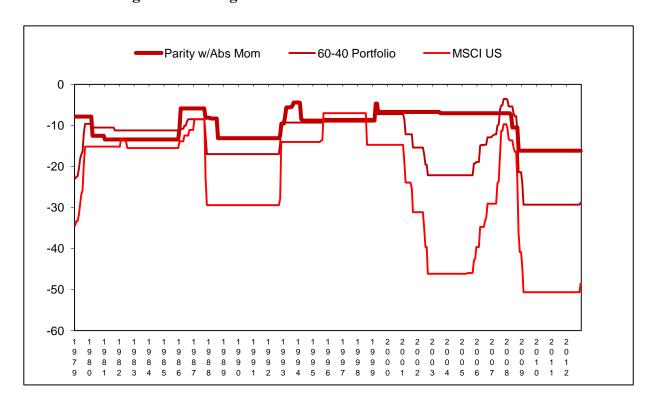


Table 7 shows how our Parity Portfolio with absolute momentum, by adapting to regime change, bypassed all of the major equity erosions of the stock market since our data began in 1974.

**Table 7 Maximum Stock Market Drawdown 1974-2012** 

| Date         | MSCI US | 60-40 Portfolio | Parity w/Abs Mom |
|--------------|---------|-----------------|------------------|
| 3/74 - 9/74  | -33.3   | -22.4           | +2.2             |
| 9/87-11/87   | -29.4   | -17.0           | -1.7             |
| 9/00 – 9/01  | -30.9   | -15.4           | +5.4             |
| 4/02 - 9/02  | -29.1   | -12.2           | +7.3             |
| 11/07 - 2/09 | -50.6   | -29.3           | -0.4             |
| 11/07 - 2/07 | -50.0   | -27.3           | - <b>0.4</b>     |

Figure 13 is a plot of our Parity Portfolio quarterly returns on the y-axis plotted against the corresponding quarterly returns of the S&P 500 index plotted on the x-axis. We can see clearly how the Parity Portfolio with absolute momentum has truncated stock market losses.

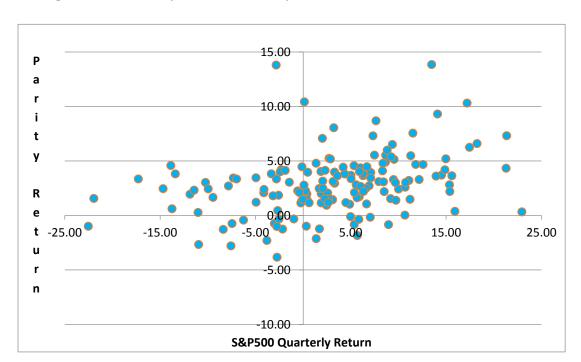


Figure 13 Quarterly Returns - Parity Portfolio versus S&P 500 1974-2012

## 8. Stochastic Dominance

Since financial markets can have non-stationary variance and auto-correlated, interdependent return distributions, it is best to analyze and compare those using robust or non-parametric methods. One such method is second-order stochastic dominance, where one set of outcomes is preferred over another if it is more predictable (less risky) and has at least as high a mean return (Hader and Russell (1969)). Figure 14 is a plot of the cumulative distribution function of the monthly returns of the Parity Portfolios, with and without absolute momentum.

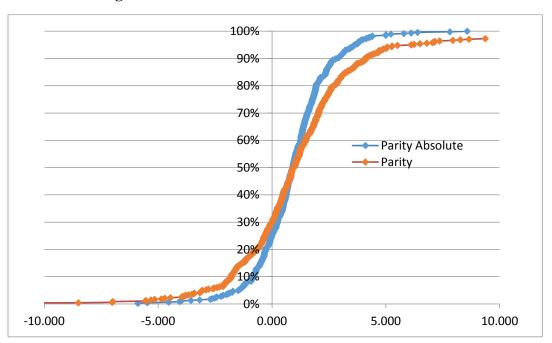


Figure 14 Cumulative Distribution Functions 1974-2012

The Parity Portfolio with 12-month absolute momentum shows a lower probability of loss and a greater probability of gain than the Parity Portfolio without momentum. Because the mean of the Parity Portfolio with 12-month absolute momentum is also higher than the mean of the Parity Portfolio without absolute momentum, a risk- averse investor would always prefer the Parity Portfolio with 12-month absolute momentum, due to second order stochastic dominance.

# 9. Leverage

Risk parity programs often have so much fixed income in their portfolios to equalize risk exposure that their managers have to leverage the portfolios in order to strive for an acceptable level of expected return. Since absolute momentum reduces the

volatility of our Parity Portfolio while, at the same, preserving equity level returns, there is not the same need for leverage.

However, given the low expected drawdown of an absolute momentum Parity Portfolio, one may still wish to use leverage in order to boost expected returns, as is done with other risk parity programs.<sup>8</sup> Table 8 shows the pro-forma results of our 12month absolute momentum Parity Portfolio leveraged to an annual volatility level just below the long-term volatility of 10.77 belonging to a normal 60-40 portfolio. We use a borrowing cost of the fed funds rate plus 25 basis points<sup>9</sup> and leverage of 1.85 to 1.

**Table 8 Parity Portfolios 1974-2012** 

|                 | Leveraged Parity<br>w/Abs Mom | Parity Portfolio<br>w/Abs Mom | Parity Portfolio<br>No Momentum |
|-----------------|-------------------------------|-------------------------------|---------------------------------|
| Annual Return   | 16.87                         | 11.98                         | 11.28                           |
| Annual Std Dev  | 10.61                         | 5.75                          | 8.88                            |
| Annual Sharpe   | .98                           | 1.06                          | .62                             |
| Max Drawdown    | -18.44                        | -9.60                         | -30.40                          |
| Skew            | .07                           | .16                           | 82                              |
| Excess Kurtosis | 2.77                          | 2.70                          | 7.04                            |

Risk in a levered portfolio has many facets, such as fat tail, illiquidity, counterparty, basis, and converging correlation risk. Since most risk parity programs have well over 50% of their assets in fixed income securities, their greatest future risk may be that

<sup>&</sup>lt;sup>8</sup> Trend following methods can also reduce negative skew and associated left tail risk (Rulle (2004)). Negative skew can be especially problematic when combined with leverage. Absolute momentum here eliminates negative skew.

<sup>9</sup> Elimination of Treasury bill holdings in lieu of borrowing would reduce borrowing costs. We have not accounted for this

cost saving.

of rising interest rates. An increase in nominal interest rates back to a historically normal level of 6% could lead to a 50% drop in the price of long bonds. Parity with 12-month absolute momentum, as presented here, is more dynamic than normal risk parity and has the ability to exit fixed income investments during periods of rising interest rates, due to its trend following nature. Absolute momentum is, in general, a valuable adjunct to the use of leverage.

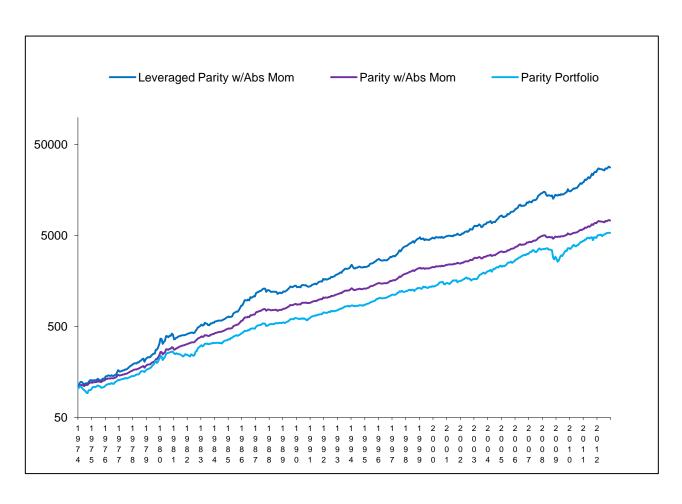


Figure 15 Parity Portfolios 1974-2012

# **10. Factor Pricing Models**

Table 9 shows our 12-month absolute momentum Parity Portfolio regressed against the U.S. stock market using the single-factor capital asset pricing model (CAPM), as well as the three-factor Fama-French model incorporating market, size, and value risk factors, as per the Kenneth French website<sup>10</sup>. We also show a four-factor Fama-French/Carhart model that adds cross-sectional momentum, and a six-factor model that additionally adds the excess return of the Barclays Capital U.S. Aggregate Bond and S&P GSCI commodity indices.

**Table 9 Factor Model Coefficients 1974-2012** 

|                                 | Annual<br>Alpha   | Market<br>Beta    | Small<br>Beta   | Value<br>Beta    | Momentum<br>Beta | Bond<br>Beta   | GSCI<br>Beta   | $R^2$ |
|---------------------------------|-------------------|-------------------|-----------------|------------------|------------------|----------------|----------------|-------|
| 6 Factor<br>Model               | 3.82***<br>(4.10) | .159***<br>(6.90) | 044<br>(1.51)   | .039<br>(1.41)   | .078*** (2.75)   | .259*** (3.28) | .045*** (4.56) | .23   |
| 4 Factor-Fama<br>French/Carhart | 4.07***<br>(4.28) | .167***<br>(7.84) | 061**<br>(2.00) | .054**<br>(2.01) | .092*** (3.39)   | -              | -              | .21   |
| 3 Factor-<br>Fama-French        | 5.24***<br>(5.99) | .149*** (6.54)    | 071**<br>(2.38) | 017<br>(0.86)    | -                | -              | -              | .17   |
| Single Factor-<br>CAPM          | 4.97***<br>(5.62) | .139*** (6.29)    | -               | -                | -                | -              | -              | .15   |

Newey-West (1987) robust t-statistics in parentheses adjust for serial correlation and possible heteroskedasticity. Statistical significance at the 1% and 5% level is denoted by \*\*\* and \*\* respectively.

Since our Parity Portfolio is long only, we naturally see highly significant loadings on the stock, bond, and GSCI market factors. Absolute momentum captures some of the cross-sectional momentum beta, which is also significant. Alphas are strong

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<sup>10</sup> http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data\_library.html

and highly significant under all four pricing models. Our Parity Portfolio with 12-month absolute momentum provides substantial and significant alphas according to all four models.

## 11. Conclusions

Cowles and Jones first presented 12-month momentum to the public in 1937. It has held up remarkably well ever since. Relative strength momentum, looking at performance against one's peers, has attracted the most attention from researchers and investors. Yet it is only a secondary way of looking at price strength. Absolute momentum, measuring an asset's performance with respect to its own past, is a more direct way of looking at and utilizing market trends to determine price continuation.

Trend determination through absolute momentum can help one navigate downside risk, take advantage of regime persistence, and achieve extraordinary risk-adjusted returns. Absolute momentum, as used here, is a simple rule-based approach that is easy to implement. One needs only see if returns relative to Treasury bills have been up or down for the preceding year.

We have seen how 12-month absolute momentum can help improve the reward-to-risk characteristics of a broad range of individual investments. Absolute momentum also has considerable value as a tactical overlay to multi-asset portfolios, where it has many potential uses. Absolute momentum can enhance the expected return and reduce the expected drawdown of core portfolios, as we have shown in this paper. It can help

investors with basic stock/bond allocations, such as the 60-40 mix, meet their investment objectives without resorting to leverage, riskier assets such as hedge funds and private placements, and complex portfolio constructs that rely heavily on the use of non-stationary correlation and covariance.

Absolute momentum can be an attractive alternative to option overwriting by retaining more of the potential for upside appreciation, while at the same time providing greater downside protection. Absolute momentum can similarly be an attractive alternative to costly tail risk hedging. It can reduce or eliminate diminishing returns from over-aggressive diversification. If one wishes to achieve higher returns by using riskier assets or by leveraging a portfolio, then 12- month absolute momentum can make that more viable by truncating expected drawdown.

Despite its many possible uses, absolute momentum has yet to attract the attention it deserves as an attractive investment strategy and risk management tool. We have developed applications for, variations of, and enhancements to 12- month absolute momentum that go beyond the scope of this introductory paper. Yet all investors would do well to become familiar with absolute momentum, since, even in its simplest form as presented here, absolute momentum can be an attractive stand-alone strategy, or a powerful tactical overlay for improving the risk-adjusted performance of most any asset or portfolio.

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